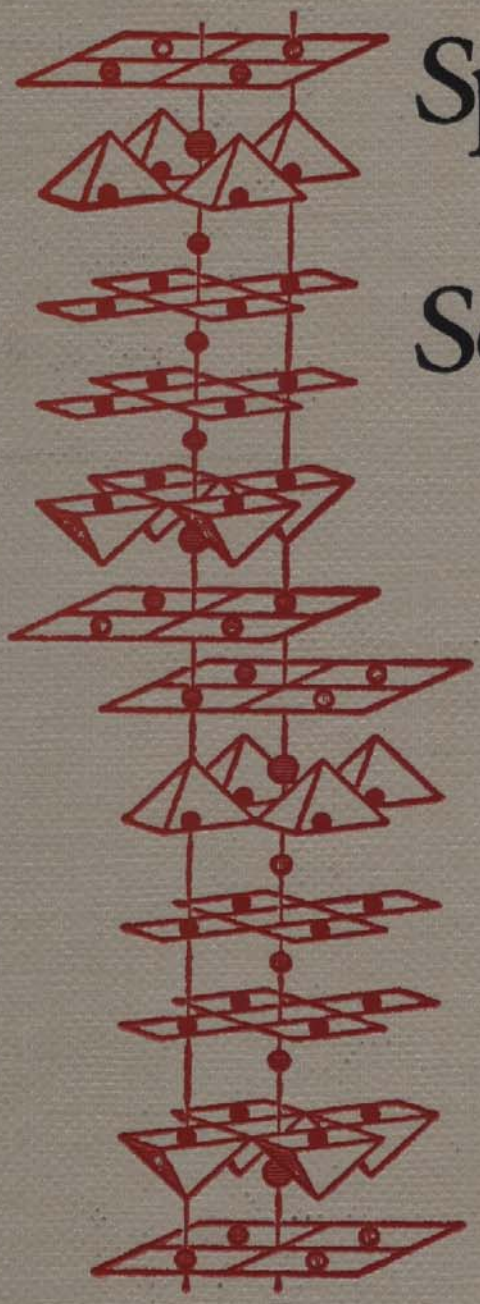

Space Groups *for* Solid State Scientists

Second Edition

GERALD BURNS
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