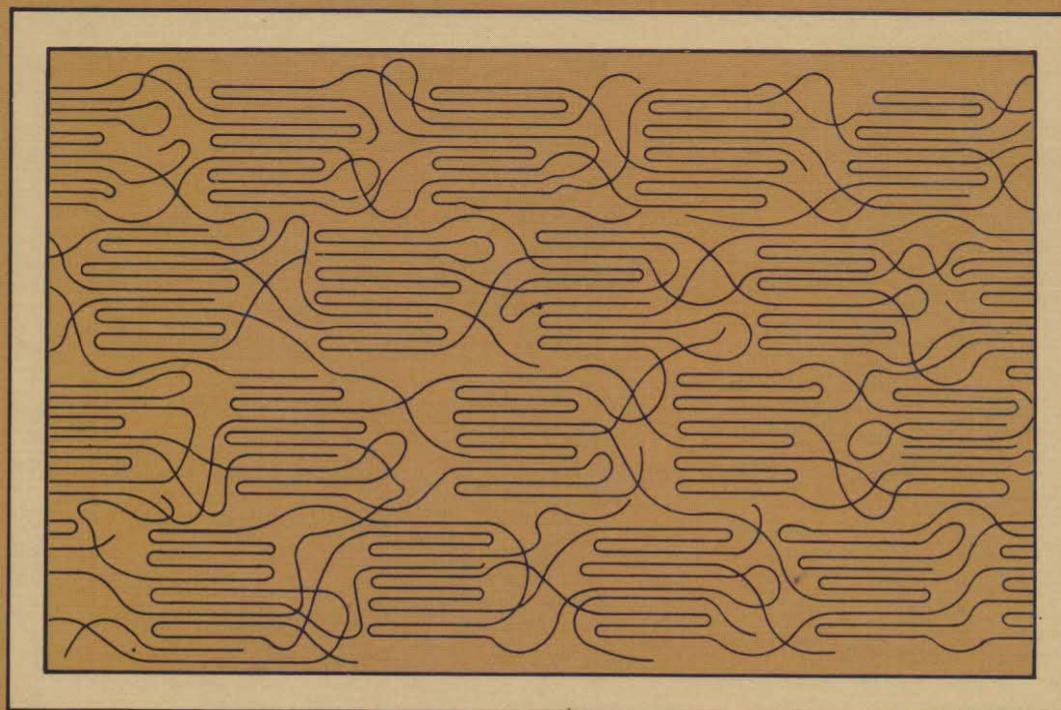


Polymer Solutions

by
Hiroshi Fujita



Studies in Polymer Science 9

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