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Applied Mathematical Sciences 114

Multiple Scale and Singular Perturbation Methods

Springer

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This book is a revised and updated version, including a substantial portion of new material, of the authors' widely acclaimed earlier text, *Perturbation Methods in Applied Mathematics* (AMS 34). A new chapter dealing with regular expansions has been added, the discussion of layer-type singular perturbations has been revised, and the coverage of multiple scale and averaging methods has been significantly expanded to reflect recent advances and viewpoints. The result is a comprehensive account of the various perturbation techniques currently used in the sciences and engineering that is suitable both as a graduate text and as a reference work on the subject.

ISBN 0-387-94202-5

ISBN 0-387-94202-5

EAN

9 780387 942025 >