

EARTH PRESSURE CALCULATION

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Application of a new Theory of Rupture
to the Calculation and Design of
Retaining Walls, Anchor Slabs, Free Sheet Walls,
Anchored Sheet Walls, Fixed Sheet Walls, Braced Walls,
Double Sheet Walls and Cellular Cofferdams

With Summaries in English and Danish

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