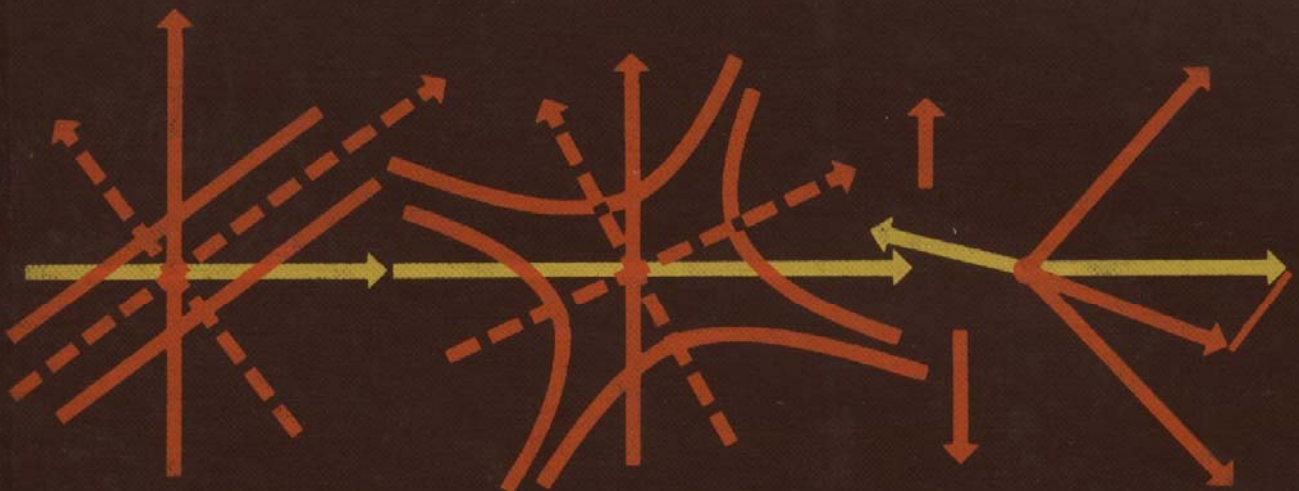


APPLIED LINEAR ALGEBRA

SECOND EDITION



BEN NOBLE / JAMES W. DANIEL

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