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# MATHEMATICAL HANDBOOK OF FORMULAS AND TABLES

**Second Edition**

**MURRAY R. SPIEGEL, Ph. D.    JOHN LIU, Ph. D.**

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