Transition, Turbulence, and Noise:

Theory and Applications for Scientists and Engineers

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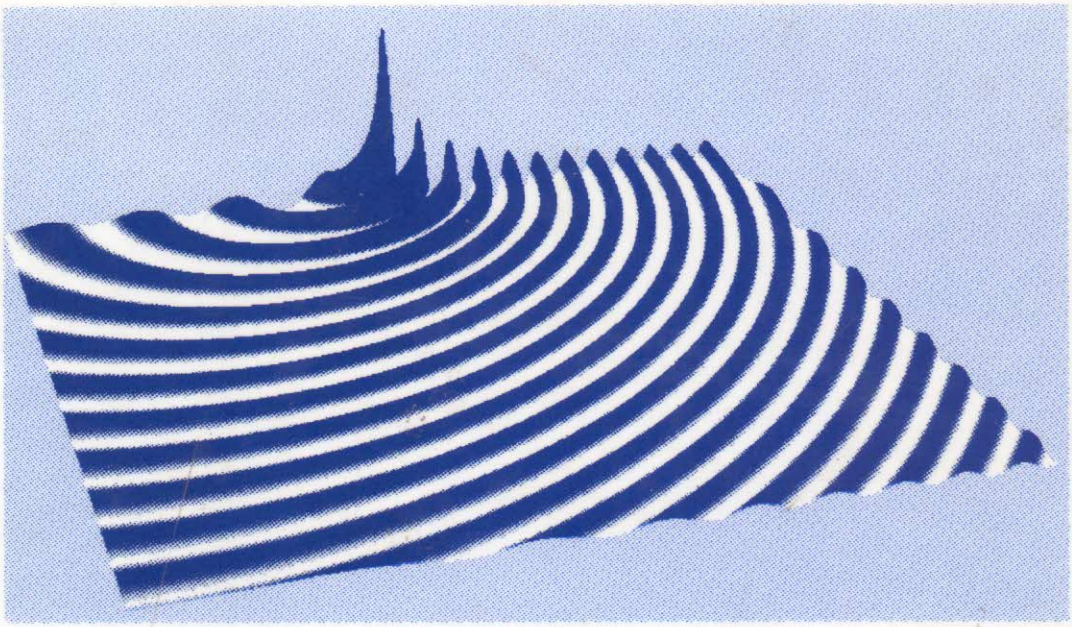

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