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INTRODUCTION TO PROBABILITY
AND STATISTICS FOR
ENGINEERS AND SCIENTISTS

WILEY SERIES IN PROBABILITY AND
MATHEMATICAL STATISTICS



Contents

CHAPTER 1.

Elements of Probability

1. Introduction	1
2. Sample Space and Events	2
3. Venn Diagrams and the Algebra of Events	4
4. Axioms of Probability	5
5. Sample Spaces Having Equally Likely Outcomes	7
6. Conditional Probability	12
7. Bayes' Formula	15
8. Independent Events	21
Problems	23

CHAPTER 2.

Random Variables and Expectation

	29
1. Random Variables	29
2. Types of Random Variables	31
3. Jointly Distributed Random Variables	35
3.1. Conditional Distributions	42
4. Expectation	44
5. Properties of the Expected Value	48
6. Variance	53
7. Covariance and Variance of Sums of Random Variables	56
8. Moment Generating Functions	60
9. Chebyshev's Inequality and the Weak Law of Large Numbers	61
Problems	63

CHAPTER 3.

Special Random Variables	71
0. Introduction	71
1. The Bernoulli and Binomial Random Variables	71
1.1. Computing the Binomial Distribution Function	76
2. The Poisson Random Variable	78
2.1. Computing the Poisson Distribution Function	84
3. The Hypergeometric Random Variable	85
4. The Uniform Random Variable	89
5. Normal Random Variables	96
5.1. Computing the Unit Normal Distribution Function and Its Inverse	102
5.2. The Central Limit Theorem	103
6. Exponential Random Variables	108
6.1. The Poisson Process	111
7. The Gamma Distribution	114
8. Distributions Arising from the Normal	117
8.1. The Chi-Square Distribution	117
8.2. The t -Distribution	120
8.3. The F Distribution	123
Problems	125

CHAPTER 4.

Sampling	133
1. Introduction	133
2. Measures of Central Tendency	134
3. Sample Variance and Sample Range	141
3.1. Computing the Sample Variance	143
4. Empirical Distribution Functions, Histograms, and Stem-and-Leaf Plots	146
5. Sampling Distributions from a Normal Population	150
5.1. Distribution of the Sample Mean	150
5.2. Joint Distribution of \bar{X} and S^2	151
6. Sampling from a Finite Set	152
Problems	155

CHAPTER 5.

Parameter Estimation	160
0. Introduction	160
1. Method of Moments Estimators	161
2. Maximum Likelihood Estimators	162

3. Interval Estimates	167
3.1. Confidence Interval for a Normal Mean When the Variance Is Unknown	171
3.2. Estimating the Difference in Means of Two Normal Populations	174
3.3. Confidence Intervals for the Variance of a Normal Distribution	179
3.4. Approximate Confidence Interval for the Mean of a Bernoulli Random Variable	180
3.5. Confidence Interval of the Mean of the Exponential Distribution	183
4. Evaluating a Point Estimator	184
5. Bayes Estimators	192
Problems	197

CHAPTER 6.

Hypothesis Testing

	204
1. Introduction	204
2. Significance Levels	205
3. Tests Concerning the Mean of a Normal Population	206
3.1. Case of Known Variance	206
3.1.1. One-Sided Tests	212
3.2. Unknown Variance: The t -Test	216
4. Testing the Equality of Means of Two Normal Populations	221
4.1. Case of Known Variances	221
4.2. Case of Unknown Variances	223
4.3. Unknown and Unequal Variances	225
4.4. The Paired t -Test	226
5. Hypothesis Tests Concerning the Variance of a Normal Population	228
5.1. Testing for the Equality of Variances of Two Normal Populations	229
6. Hypothesis Tests in Bernoulli Populations	230
6.1. Testing the Equality of Parameters in Two Bernoulli Populations	232
6.1.1. Computations for the Fisher-Irwin Test	233
7. Tests Concerning the Mean of a Poisson Distribution	235
7.1. Testing the Relationship Between Two Poisson Parameters	236
Problems	237

CHAPTER 7.

Regression

	245
1. Introduction	245
2. Least Squares Estimators of the Regression Parameters	247
3. Distribution of the Estimators	249
4. Statistical Inferences about the Regression Parameters	254
4.1. Inferences Concerning β	255
4.2. Inferences Concerning α	258

4.3. Inferences Concerning the Mean Response $\alpha + \beta x$	258
4.4. Prediction Interval of a Future Response	260
4.5. Summary of Distributional Results	262
5. Index of Fit	263
6. Analysis of Residuals: Assessing the Model	264
7. Transforming to Linearity	266
8. Weighted Least Squares	270
9. Polynomial Regression	275
10. Multiple Linear Regression	278
10.1. Predicting Future Responses	287
Problems	290

CHAPTER 8.

Analysis of Variance 306

1. Introduction	306
2. One-way Analysis of Variance	307
3. One-way Analysis of Variance with Unequal Sample Sizes	316
4. Two-way Analysis of Variance	317
5. Two-way Analysis of Variance with Interaction	324
Problems	331

CHAPTER 9.

Goodness of Fit and Nonparametric Testing 338

0. Introduction	338
1. Goodness of Fit Tests	338
2. Goodness of Fit Tests when All Parameters Are Specified	339
2.1. Determining the Critical Region by Simulation	345
3. Goodness of Fit Tests when Some Parameters Are Unspecified	348
3.1. Tests of Independence in Contingency Tables	350
3.2. Using Simulation	353
4. Nonparametric Tests	354
5. The Sign Test	354
6. The Signed Rank Test	356
7. The Two-sample Problem	361
7.1. The Classical Approximation and Simulation	366
8. The Run Test for Randomness	369
Problems	372

CHAPTER 10.

Life Testing 380

1. Introduction	380
2. Hazard Rate Functions	380

3. The Exponential Distribution in Life Testing	383
3.1. Simultaneous Testing-stopping at the r th Failure	383
3.2. Sequential Testing	387
3.3. Simultaneous Testing-stopping by a Fixed Time	391
3.4. The Bayesian Approach	393
4. A Two-sample Problem	394
5. The Weibull Distribution in Life Testing	396
5.1. Parameter Estimation by Least Squares Problems	398
	400

CHAPTER 11.

Quality Control

406

1. Introduction	406
2. Control Charts for Average Values: The \bar{X} -Control Charts	407
2.1. Case of Unknown μ and σ	410
3. S -Control Charts	415
4. Control Charts for Fraction Defective	417
5. Control Charts for Number of Defects	420
6. Other Control Charts for Detecting Changes in the Population Mean	423
6.1. Moving-Average Control Charts	423
6.2. Exponentially Weighted Moving-Average Control Charts	425
Problems	429

CHAPTER 12.

Simulation

436

1. Introduction	436
2. General Techniques for Simulating Continuous Random Variables	442
2.1. The Inverse Transformation Method	442
2.2. The Rejection Method	443
3. Simulating from Discrete Distributions	447
4. Variance Reduction Techniques	450
4.1. Use of Antithetic Variables	451
4.2. Control Variates	454
Problems	455

Appendix of Programs

459

Appendix of Tables

481

Answers to Selected Problems

487

Index

489

