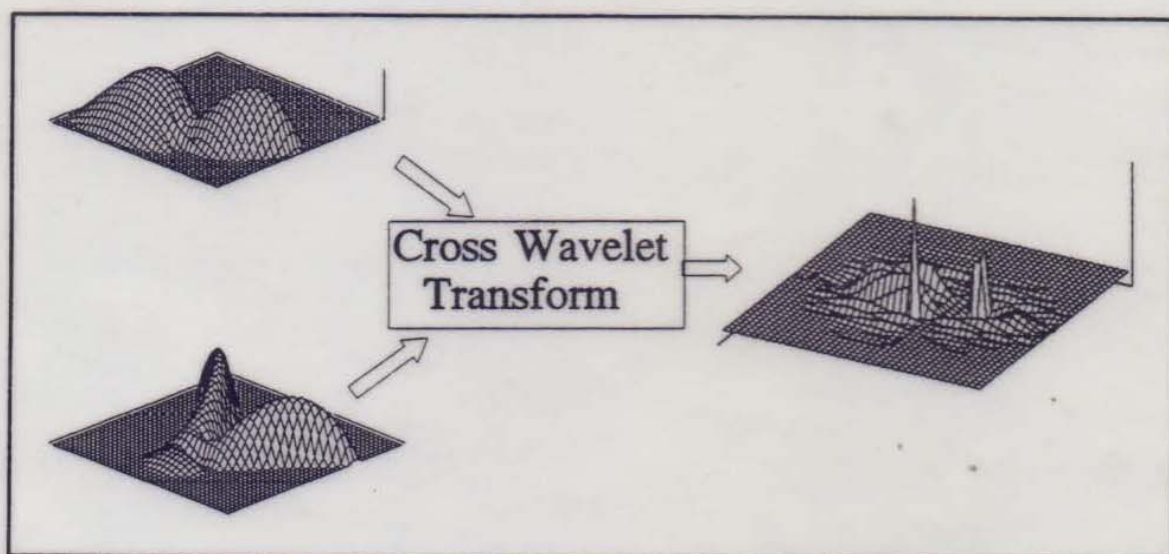

WAVELET THEORY AND ITS APPLICATIONS

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foreword by N.K. Bose



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