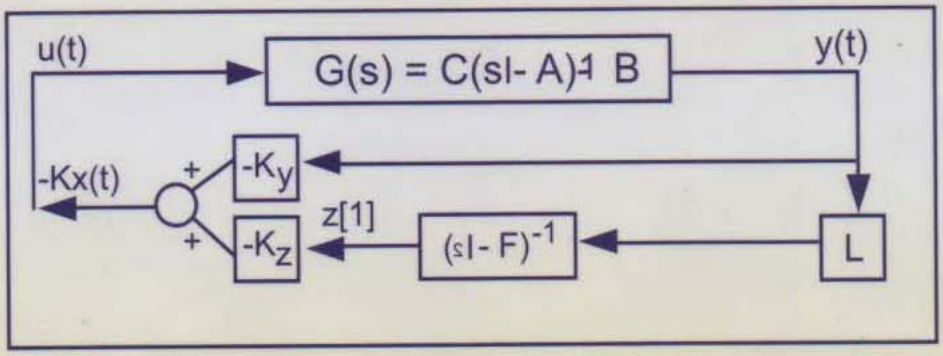
Control Engineering Series

Robust Control System Design

Advanced State Space Techniques

Second Edition, Revised and Expanded



Chia-Chi Tsui

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