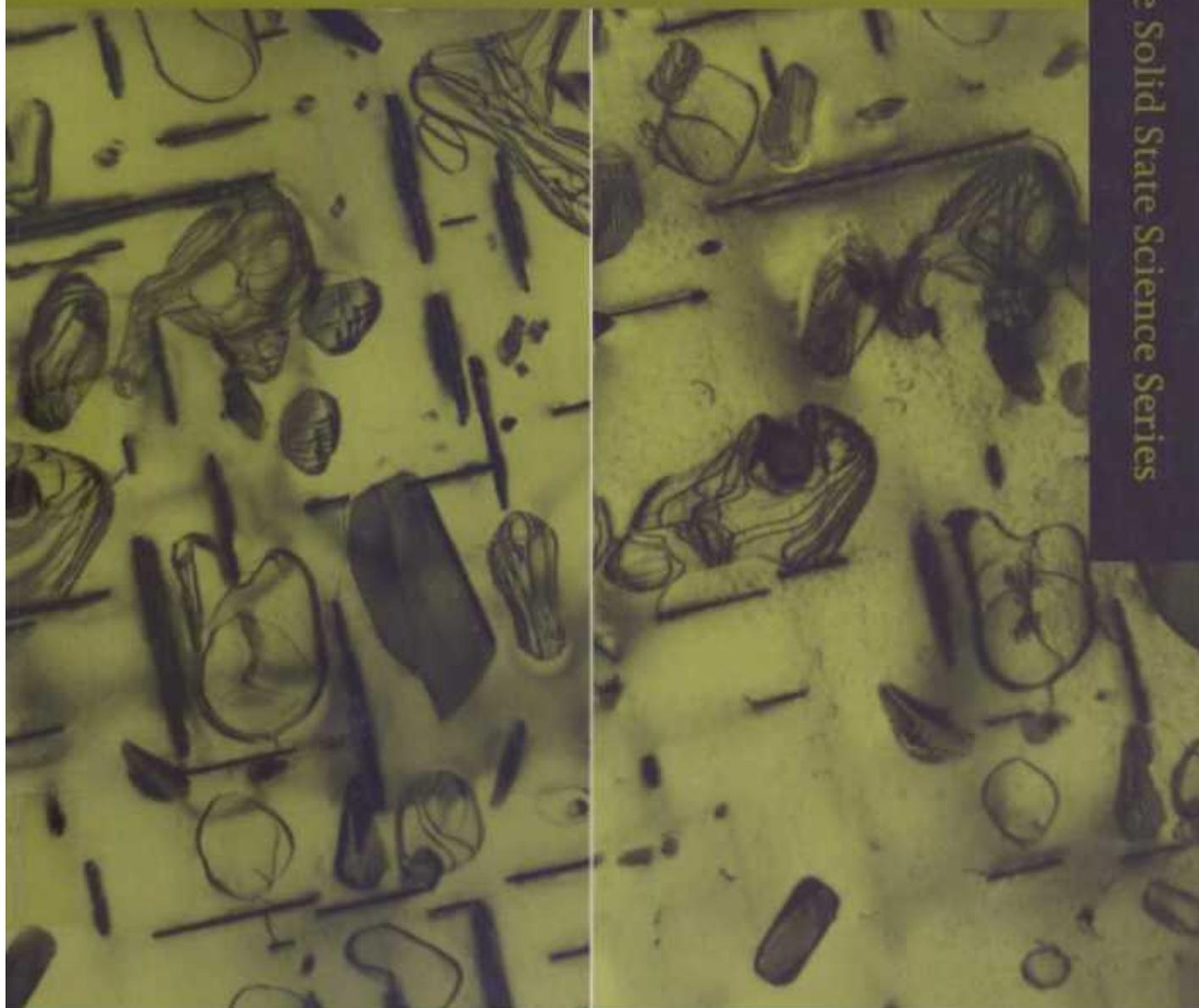


2

Mass Transport in Solids and Fluids

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Cambridge Solid State Science Series



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