

# THEORY AND PHENOMENOLOGY of **Sparticles**

An account of four-dimensional  $N=1$   
supersymmetry in High Energy Physics

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