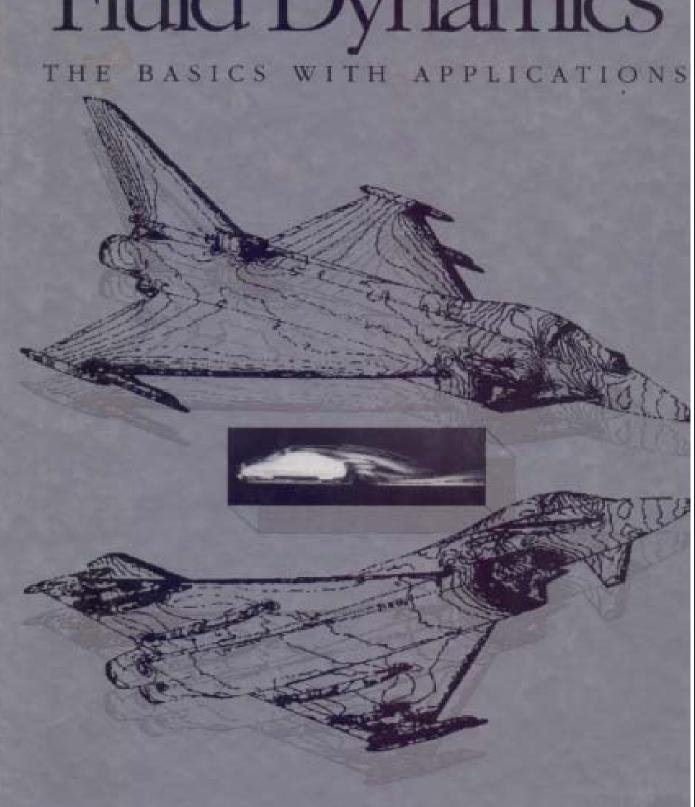
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## Computational Fluid Dynamics



## CONTENTS

Part I	Preface Basic Thoughts and Equations	xix
1	Philosophy of Computational Fluid Dynamics  1.1 Computational Fluid Dynamics: Why? 1.2 Computational Fluid Dynamics as a Research Tool 1.3 Computational Fluid Dynamics as a Design Tool 1.4 The Impact of Computational Fluid Dynamics—Some Other Examples 1.4.1 Automobile and Engine Applications 1.4.2 Industrial Manufacturing Applications 1.4.3 Civil Engineering Applications 1.4.4 Environmental Engineering Applications 1.4.5 Naval Architecture Applications (Submarine Example) 1.5 Computational Fluid Dynamics: What Is It? 1.6 The Purpose of This Book	3 4 6 9 13 14 17 19 20 22 23 32
2	The Governing Equations of Fluid Dynamics: Their Derivation, a Discussion of Their Physical Meaning, and a Presentation of Forms Particularly Suitable to CFD  2.1 Introduction 2.2 Models of the Flow 2.2.1 Finite Control Volume 2.2.2 Infinitesimal Fluid Element 2.2.3 Some Comments  2.3 The Substantial Derivative (Time Rate of Change Following a Moving Fluid Element 2.4 The Divergence of the Velocity: Its Physical Meaning 2.4.1 A Comment	37 38 40 41 42 42 43 47 48

	2.5		49
		2.5.1 Model of the Finite Control Volume Fixed in Space	49
		2.5.2 Model of the Finite Control Volume Moving with the	51
		2.5.3 Model of an Infinitesimally Small Element Fixed	31
		in Space	53
		2.5.4 Model of an Infinitesimally Small Fluid Element	100
		Moving with the Flow	55
		2.5.5 All the Equations Are One: Some Manipulations	56
		2.5.6 Integral versus Differential Form of the Equations:	
		An Important Comment	60
	2.		60
	2.		66
	2		
		With Comments	75
		2.8.1 Equations for Viscous Flow (the Navier-Stokes	
		Equations)	75
		2.8.2 Equations for Inviscid Flow (the Euler Equations)	77
		2.8.3 Comments on the Governing Equations	78
	2.	9 Physical Boundary Conditions	80
	2	10 Forms of the Governing Equations Particularly Suited for	
		CFD: Comments on the Conservation Form, Shock Fitting,	
		and Shock Capturing	82
	2.	11 Summary	92
		Problems	93
	3 N	Iathematical Behavior of Partial Differential	
			95
		quations: The Impact on CFD	95
	3.		97
	3.		71
	3.	Partial Differential Equations: The Eigenvalue Method	102
	3.		100
	- 2	Differential Equations: Impact on Physical and	
		Computational Fluid Dynamics	105
		3.4.1 Hyperbolic Equations	106
		3.4.2 Parabolic Equations	111
		3.4.3 Ellintic Equations	117
		3.4.4 Some Comments: The Supersonic Blunt Body	530
		Problem Revisited	119
	3.	5 Well-Posed Problems	120
	3.		121
		Problems	121
Part	H F	Basics of the Numerics	
	OR STATE OF		_
	4 B	asic Aspects of Discretization	125
	100	THE PARTY OF THE P	And the second
	4.	.1 Introduction 2 Introduction to Finite Differences	125 128

	CONTENTS	xiii
	4.3 Difference Equations	142
	4.4 Explicit and Implicit Approaches: Definitions and Contrasts	145
	4.5 Errors and an Analysis of Stability	153
	4.5.1 Stability Analysis: A Broader Perspective	165
	4.6 Summary	165
	GUIDEPOST	166
	Problems	167
		The
5	Grids with Appropriate Transformations	168
	5.1 Introduction	168
	5.2 General Transformation of the Equations	171
	5.2 Metries and Jacobians	178
	5.4 Form of the Governing Equations Particularly Suited	
	for CFD Revisited: The Transformed Version	183
	5.5 A Comment	186
	5.6 Stretched (Compressed) Grids 5.7 Boundary-Fitted Coordinate Systems; Elliptic Grid	186
	Generation	192
	GUIDEPOST	193
	5.8 Adaptive Grids	200
	5.8 Adaptive Grids 5.9 Some Modern Developments in Grid Generation	208
	5.10 Some Modern Developments in Finite-Volume Mesh	200
	Generation: Unstructured Meshes and a Return to Cartesian	210
	Meshes	210
	5.11 Summary	215
	Problems	213
6	Some Simple CFD Techniques: A Beginning	216
	6.1 Introduction	216
	6.2 The Lax-Wendroff Technique	217
	6.3 MacCormack's Technique	222
		223
	GUIDEPOST	150
	6.4 Some Comments: Viscous Flows, Conservation Form,	-
	and Space Marching	225
	6.4.1 Viscous Flows	225
	6.4.2 Conservation Form	225
	6.4.3 Space Marching	226
	6.5 The Relaxation Technique and Its Use with Low-Speed	70000
	Inviscid Flow	229
	6.6 Aspects of Numerical Dissipation and Dispersion; Artificial	- Legentrasia
	Viscosity	232
	6.7 The Alternating-Direction-Implicit (ADI) Technique	243
	6.8 The Pressure Correction Technique: Application	
	to Incompressible Viscous Flow	247
7	6.8.1 Some Comments on the Incompressible	
	Navier-Stokes Equations	248

market 1	
3.30	CONTRACTS

		10.3.4 Calculation of Step Stzes in Space and Time	433
		10.3.5 Initial and Boundary Conditions	457
		10.4 Organization of Your Navier-Stokes Code	459
		10.4.1 Overview	459
		10.4.2 The Main Program	461
		10.4.3 The MacCormack Subroutine	463
		10.4.4 Final Remarks	466
		10.5 Final Numerical Results: The Steady State-Solution	466
		10.6 Summary	474
Part	ΙV	Other Topics .	
	11	Some Advanced Topics in Modern CFD:	
		A Discussion	479
		11.1 Introduction	479
		TILL TROUGHTENING	7/3
		11.2 The Conservation Form of the Governing Flow Equations	480
		Revisited: The Jacobians of the System	482
		11.2.1 Specialization to One-Dimensional Flow	
		11.2.2 Interim Summary	489
		11.3 Additional Considerations for Implicit Methods	489
		11.3.1 Linearization of the Equations: The Beam and Warming Method	490
		11.3.2 The Multidimensional Problem: Approximate	
		Factorization	492
		11.3.3 Block Tridiagonal Matrices	496
		11.3.4 Interim Summary	497
		11.4 Upwind Schemes	497
		11.4.1 Flux-Vector Splitting	500
		11.4.2 The Godunov Approach	502
		11.4.3 General Comment	507
		11.5 Second-Order Upwind Schemes	507
		11.6 High-Resolution Schemes: TVD and Flux Limiters	509
		11.7 Some Results	510
		11.8 Multigrid Method	513
		11.9 Summary	514
		Problems	514
	12	The Future of CFD	515
		12.1 The Importance of CFD Revisited	515
		12.2 Computer Graphics in CFD	516
		12.3 The Future of CFD: Enhancing the Design Process	517
		12.4 The Future of CFD: Enhancing Understanding	526
	14	12.5 Conclusion	533
1985			

10.3.3 The Finite-Difference Equations

453

	CONTENTS	xvii
Appendix A Solution of a	Thomas' Algorithm for the Tridiagonal System of Equations	534
References		539
Index		543