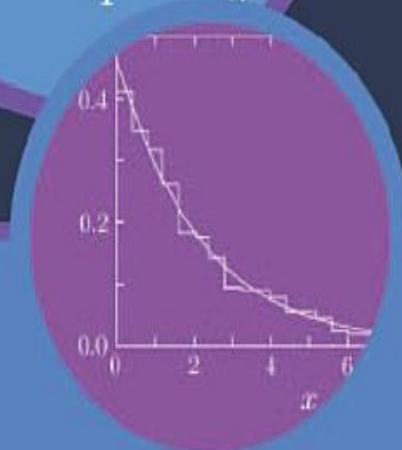
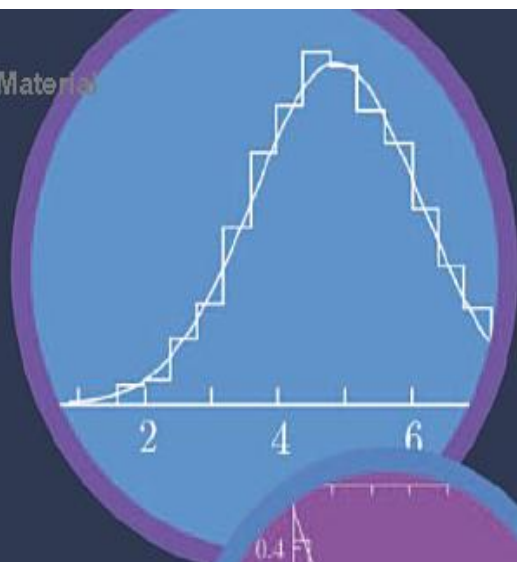
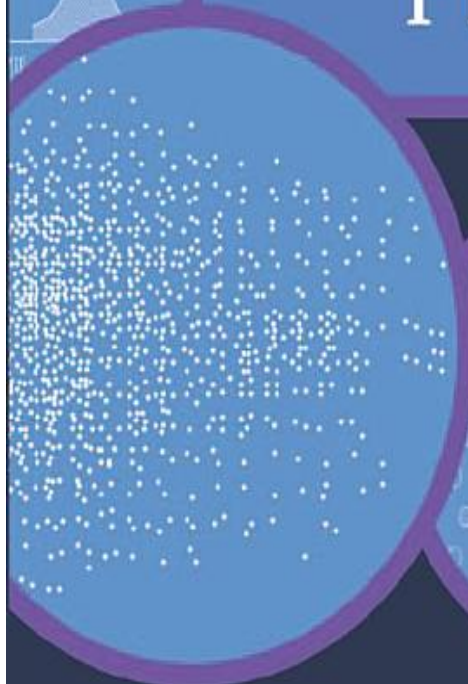


Second Edition

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Probability and Statistics for Physical Sciences



Brian R. Martin and Mark F. Hurwitz



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PROBABILITY AND STATISTICS FOR PHYSICAL SCIENCES

SECOND EDITION

BRIAN R. MARTIN
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