



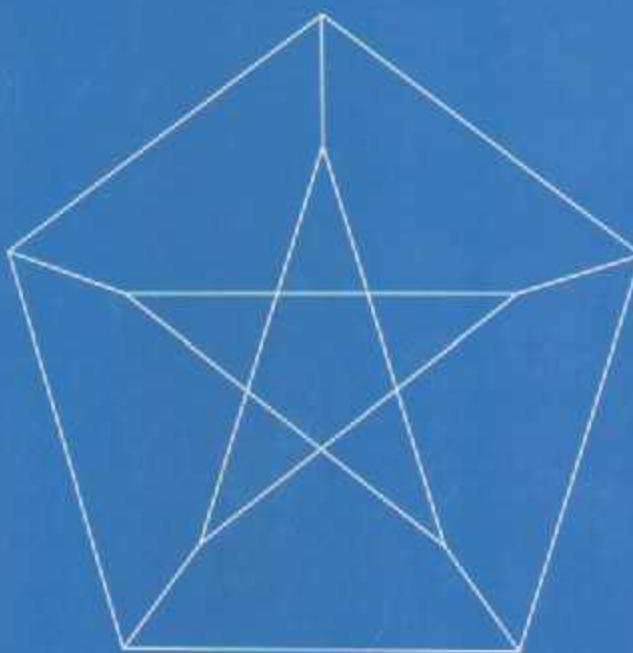
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# DISCRETE MATHEMATICS



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## Lower bounds for lower independence and domination numbers in graphs

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In this paper we prove some lower bounds for the lower independence number and the lower domination number of a graph. We also prove that if  $G$  is a connected graph with at least two vertices, then  $\gamma^-(G) \geq \gamma(G) - 1$ . Moreover, we prove that if  $G$  is a connected graph with at least two vertices, then  $\alpha^-(G) \geq \alpha(G) - 1$ . Finally, we prove that if  $G$  is a connected graph with at least two vertices, then  $\gamma^-(G) \geq \alpha^-(G)$ . These results generalize the previously known lower bounds for the upper independence number and the upper domination number.

Keywords:

lower independence number; lower domination number; graph theory

### 1. Introduction

The concepts of independence and domination in graphs have been studied by many researchers in graph theory [1–10]. In addition to these two concepts, domination and independence, there are other concepts such as lower domination and lower independence which are closely related to the concepts of domination and independence. The lower domination number of  $G$  is the minimum size of a dominating set of  $G$  [11].



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