

Second Edition

DIGITAL FILTER DESIGNER'S HANDBOOK

**With C++
Algorithms**

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**DISK
Included**



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