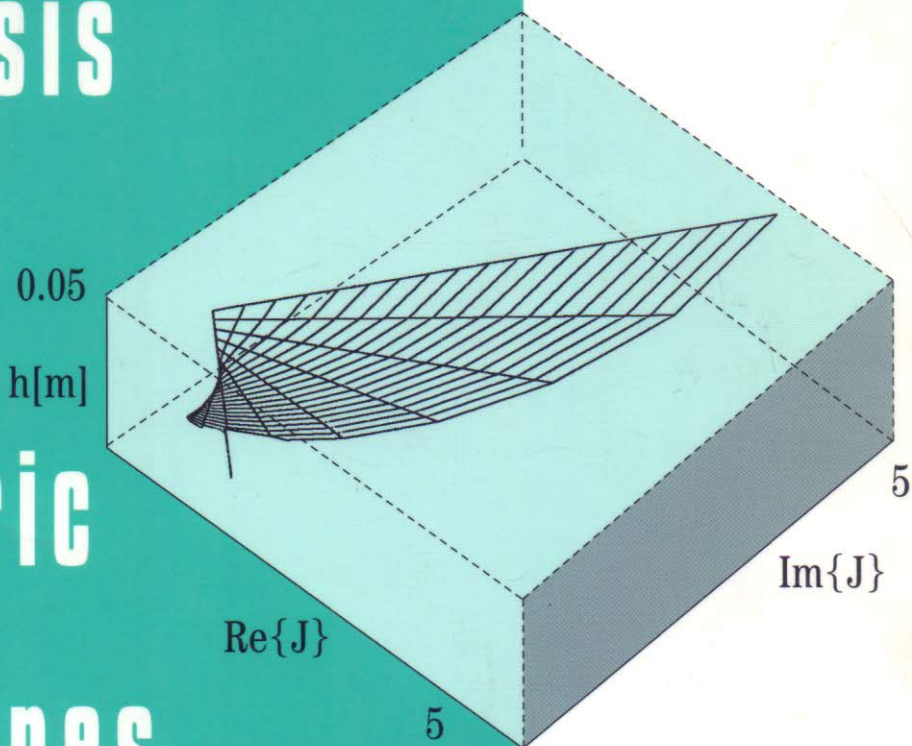


Computer-  
aided  
Analysis  
of  
Electric  
Machines

*A Mathematica  
approach*



*Vlado  
Ostovic*

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