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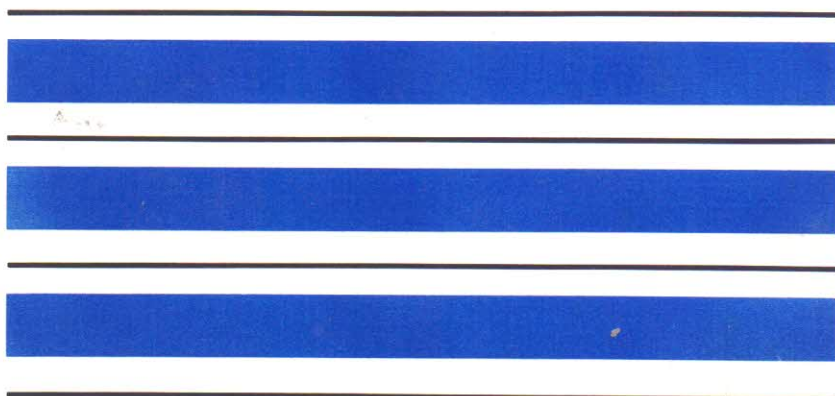
# **Asymptotic Waveform Evaluation**

**And Moment Matching  
for Interconnect Analysis**

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