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**DYNAMIC**

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**ANALYSIS AND**

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**EARTHQUAKE**

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**RESISTANT**

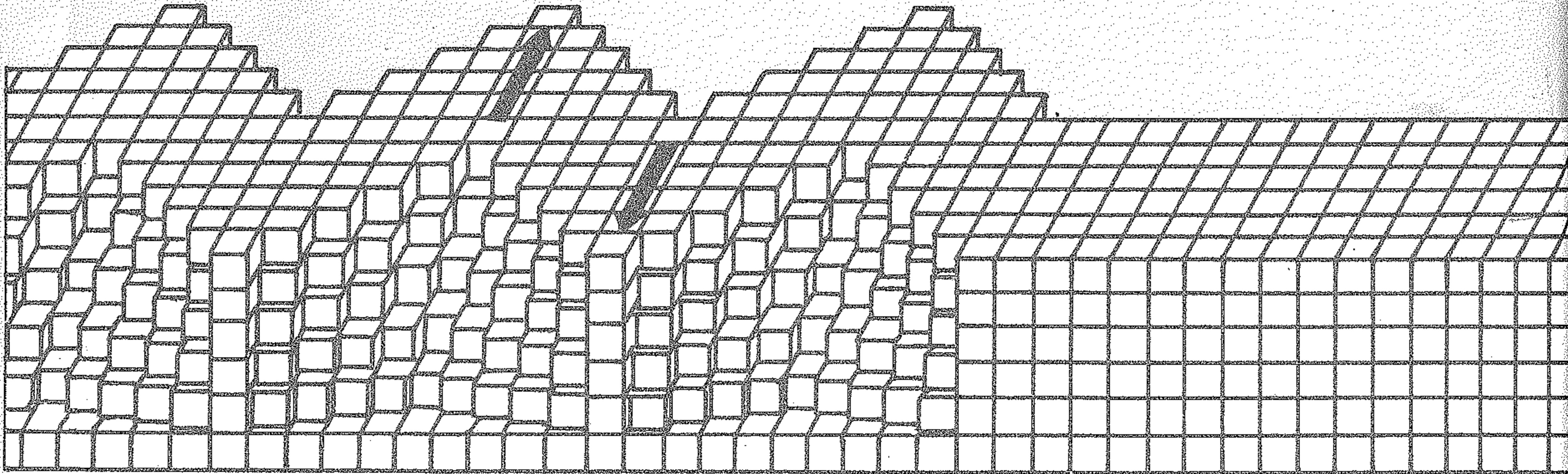
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**DESIGN**

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VOLUME 2

Methods of Dynamic Analysis



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Japanese Society of Civil Engineers

# CONTENTS

PREFACE TO SERIES	v
PREFACE TO VOLUME 2	xi

## PART III METHODS OF DYNAMIC ANALYSIS

CHAPTER 1: TYPES OF NUMERICAL ANALYSIS METHODS AND THEIR CHARACTERISTICS	3
1.1 Outline	3
1.2 Continuous Mass System and Lumped Mass System	4
1.2.1 Continuous mass system	5
1.2.2 Lumped mass system	8
1.3 Finite Element Method	9
1.3.1 Formulation of equations of motion using the principle of virtual work	10
1.3.2 Finite elements of various types	14
1.4 Calculus of Finite Differences Method	17
1.4.1 Difference approximation	17
1.4.2 Finite difference method for equation of motion of an elastic body	21
1.4.3 Boundary conditions	23
1.4.4 Stability	25
1.4.5 Treatment of a boundary with an arbitrary shape	25
1.4.6 Treatment of an artificial boundary	27
1.5 Boundary Element Method	27
1.5.1 Integral transform method	27
1.5.2 Time stepping method	33
1.5.3 Numerical analysis	36

CHAPTER 2: BASIC METHODS FOR RESPONSE CALCULATIONS	41
2.1 Outline	41
2.2 Analysis of Eigenvalues	41
2.2.1 Equations to solve the eigenvalue problems	41
2.2.2 Computation of eigenvalues of a real matrix	44
2.2.3 Computation of eigenvalues of complex matrix	46
2.3 Modal Analysis Method	46
2.3.1 Discrete system	46
2.3.2 Continuous system	49
2.4 Direct Integration Method for Equation of Motion	51
2.4.1 Central difference method	52
2.4.2 Explicit method and implicit method	53
2.4.3 Integration in standard form	55
2.4.4 Implicit method for equation of motion	57
2.4.5 Summary of direct integration method	60
2.5 Analysis of Frequency Domain	61
2.5.1 Unit impulse response and frequency response function	61
2.5.2 Response under action of arbitrary external force	62
2.5.3 Fourier spectrum	63
2.5.4 Fast fourier transform (FFT)	64
2.6 Analysis of Random Response	69
2.6.1 Basics of random response analysis	69
2.6.2 Power spectrum and spectral density function	70
2.6.3 Autocorrelation function and power spectrum density function	71
2.6.4 Relation between power spectrum density function of an external force and the response	73
2.6.5 Mutual correlation function and response of a vibrating system	73
2.6.6 Physical spectrum	74
2.7 Response Spectrum	75
2.7.1 Linear response spectrum	75
2.7.2 Inelastic response spectrum	78
CHAPTER 3: NONLINEAR PROBLEM	79
3.1 Concept of Nonlinear Vibrations	79
3.2 Equivalent Linearization Method	80
3.2.1 Background of equivalent linearization method	80
3.2.2 Kryloff-Bogoliuboff analysis of forced vibrations	82
3.2.3 Damping constant of a vibrating system with an arbitrary viscoelastic restoration force	84

3.2.4	Equivalent viscous damping factor of a vibration system with arbitrary hysteretic properties	86
3.2.5	Effect of variations in definition of equivalent linear spring on response	93
3.2.6	Detailed sequence in equivalent linearization method	95
3.2.7	Meaning of damping factor used in equivalent linearization method in accordance with vibration theory	97
3.2.8	Studies on appropriateness of equivalent linearization method	100
3.3	Dynamic Analysis Based on Material Nonlinearities	103
3.3.1	Nonlinear elasticity	106
3.3.2	Elastoplasticity and viscoelasticity	106
3.3.3	Change in stiffness due to cracks	109
3.3.4	Play, separation, fusion, sliding	111
3.3.5	Solution of equation of motion using material nonlinearities	111
3.4	Dynamic Analysis Based on Finite Deformation	112
3.4.1	Lagrangian method and Euler method	113
3.4.2	Total Lagrangian method and updated Lagrangian method	113
CHAPTER 4: DYNAMIC ANALYSIS OF SOIL-STRUCTURE INTERACTION SYSTEM		116
4.1	Expression for Mutual Dynamic Interaction	116
4.1.1	Governing equation using relative coordinates	117
4.1.2	Governing equation based on absolute coordinates	120
4.2	Analysis Based on Finite Element Method	122
4.2.1	Setting boundary conditions at the artificial boundary	123
4.2.2	Analysis of whole soil-structure interaction system	127
4.2.3	Analysis of soil-structure interaction system when sliding and/or separation occur	129
4.3	Analysis Using Boundary Element Method	132
4.3.1	Direct method	132
4.3.2	Indirect method	135
4.4	Hybrid Analysis Based on Finite Element Method and Boundary Element Method	138
4.4.1	Boundary element method	139
4.4.2	Volume method (Displacement Green's function method)	142

4.5 Complete Analysis Method and Substructure Analysis Method	145
4.5.1 Complete analysis method	147
4.5.2 Dynamic substructure analysis method	153
REFERENCES	161

## PART IV DYNAMIC ANALYSIS OF THE GROUND AND FOUNDATION

CHAPTER 1: INPUT GROUND MOTION	171
1.1 Seismic Bed Rock	171
1.1.1 Considerations of seismic bed rock	171
1.1.2 Setting the seismic bed rock	172
1.1.3 Incident wave at seismic bed rock and its spectrum	174
1.2 Underground Distribution of Earthquake Motion	178
1.2.1 Measurement of underground earthquake motion	178
1.2.2 Underground earthquake motion distribution according to wave theory	181
1.3 Intensity of Earthquake Motion at Ground Surface	187
1.3.1 Peak value of earthquake motion and response spectrum	187
1.3.2 Maximum values of earthquake motion in far field	190
1.3.3 Maximum values of earthquake motion in near field	191
1.4 Propagation of Seismic Wave and Phase Difference	193
1.4.1 Phase difference of ground motion	193
1.4.2 Examples of array observations	196
1.4.3 Handling phase difference of ground motion in earthquake-resistant design	200
CHAPTER 2: SEISMIC ANALYSIS OF GROUND AND SOIL STRUCTURE	202
2.1 Methods of Dynamic Response Analysis of Horizontally Multilayer Ground and Its Behavior during an Earthquake	202
2.1.1 Multiple reflections analysis of an SH wave using a propagation matrix	203
2.1.2 Multiple-reflection theory when P and SV waves are present	206

2.1.3	Analysis with respect to surface wave	207
2.1.4	Analysis of unidimensional ground motion using equivalent linearization method	208
2.1.5	Factors affecting earthquake response characteristics of layered ground	210
2.1.6	Example of nonlinear response analysis of layered ground	211
2.1.7	Modeling nonlinear amplification characteristics of the surface	213
2.2	Earthquake Motion Analysis of Ground with Irregular Topography	215
2.2.1	Relation between irregular topography and earthquake damage	215
2.2.2	Characteristics of irregular topography determined from earthquake observations	218
2.2.3	Distinctive features of methods of analysis and examples	221
2.2.4	Points of caution in modeling irregular ground	229
2.3	Seismic Motion Analysis of Soil Structures	231
2.3.1	Typical vibration modes	232
2.3.2	Equivalent radiation damping	235
2.3.3	Superposition of model response	237
<b>CHAPTER 3: RUPTURE OF GROUND DUE TO EARTHQUAKE AND ITS PREDICTION</b>		<b>239</b>
3.1	Types of Ground Rupture	239
3.2	Liquefaction of Sandy Ground	240
3.2.1	Methods of predicting liquefaction	240
3.2.2	Prediction of liquefaction potential	240
3.2.3	Prediction of liquefaction based on dynamic analysis	241
3.2.4	Examples of effective stress analysis	244
3.2.5	Prediction of liquefaction by effective stress analysis and total stress analysis	245
3.3	Slope Failure	247
3.3.1	Types of prediction methods	247
3.3.2	Prediction methods for multiple slopes in a given region	247
3.3.3	Prediction based on individual slopes	248
3.3.4	Prediction of stability against slide using seismic intensity method	249
3.3.5	Detailed analysis of safety against slide Method 1: Evaluation of safety for entire soil mass	249
3.3.6	Detailed analysis of safety against slide Method 2: Evaluation of safety for local area	251

3.3.7 Simple method for analyzing extent of deformation	251
3.3.8 Method for detailed analysis of deformation	253
3.3.9 Analysis of slope rupture	255
CHAPTER 4: ANALYSIS OF DYNAMIC INTERACTION BETWEEN GROUND AND FOUNDATION OF A STRUCTURE	258
4.1 Dynamic Interaction	258
4.1.1 Records of acceleration observed in ground and in structure	258
4.1.2 Definition of dynamic interaction and dynamic properties	259
4.1.3 Brief historical review	262
4.2 Considerations of an Analytical Model	264
4.2.1 Basis of an analytical model	264
4.2.2 Linear model and nonlinear model	265
4.2.3 Properties of impedance	267
4.2.4 Complex stiffness and additional mass	267
4.2.5 Assuming frequency independent complex stiffness	270
4.2.6 Properties of effective earthquake input motion	271
4.3 Effect of Dynamic Interaction	272
4.4 Design Guidelines and Dynamic Interaction	276
4.4.1 Current status of design guidelines	276
4.4.2 Considerations in ATC-3	277
4.4.3 Simple method of analysis—1	278
4.4.4 Simple method of analysis—2	280
4.4.5 Dynamic interaction of pile foundation	281
4.4.6 Foundation design	282
4.5 Examples of Detailed Analysis and Calculations	283
4.5.1 Effect of embedment depth and of effective earthquake input motion	283
4.5.2 Complex stiffness	287
4.5.3 Effective earthquake input motion	289
REFERENCES	295
INDEX	303