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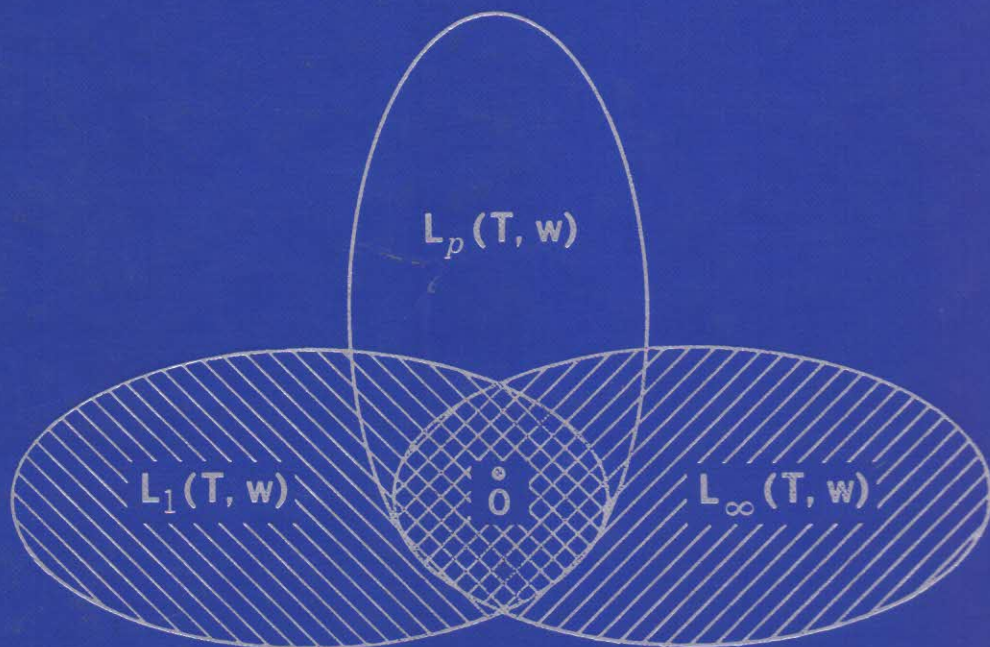
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# ENGINEERING ANALYSIS

A Vector Space  
Approach

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