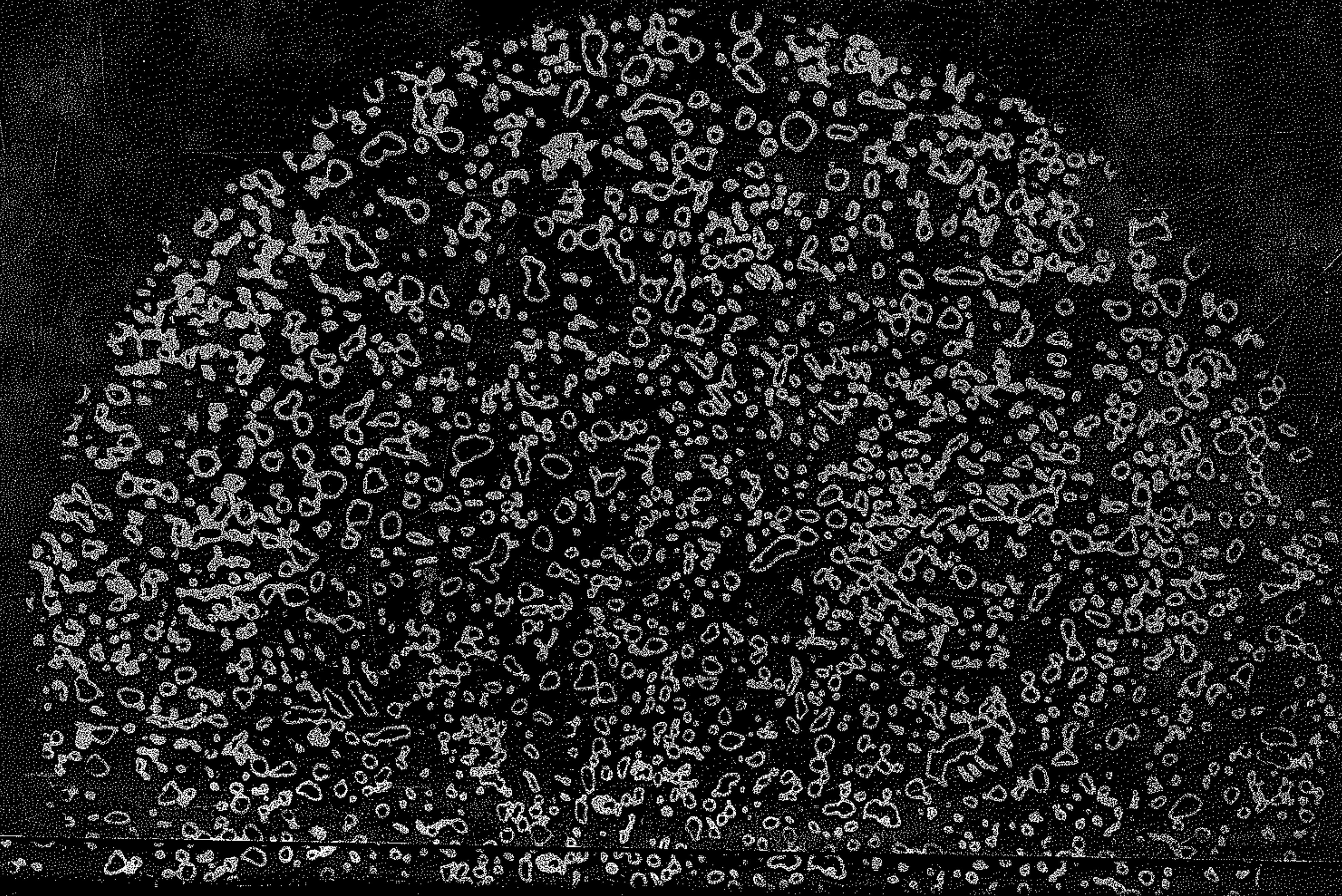


METALWORKING  
SCIENCE AND  
ENGINEERING  
EDWARD M. MIELNIK



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# METALWORKING SCIENCE AND ENGINEERING

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