
Variable
speed
electric
drives

Volume 1

Reminders of electrical
and mechanical theory,
methods of variable speed control

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