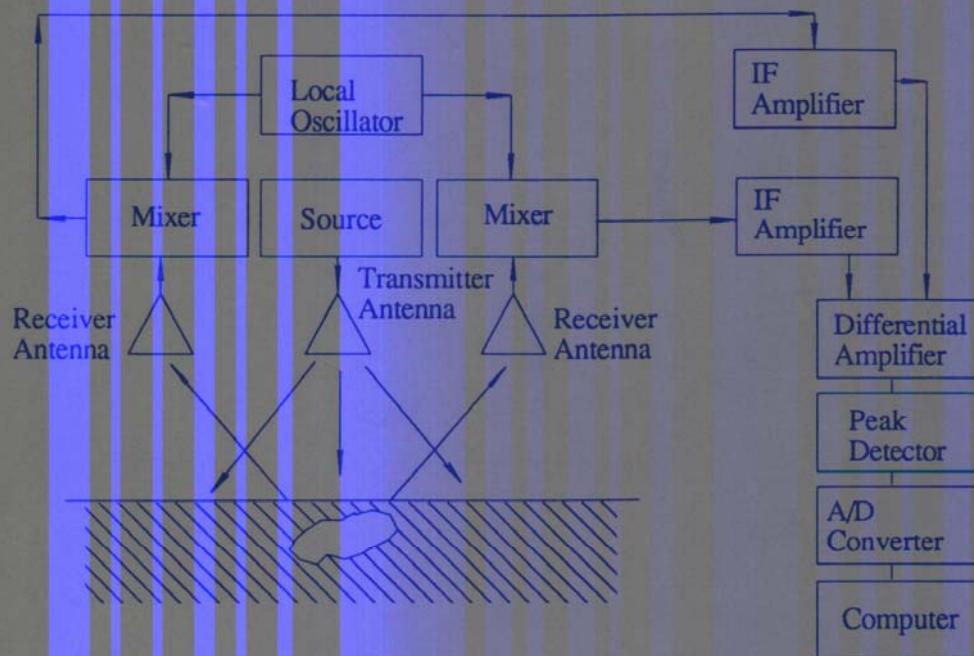


DEVELOPMENTS IN ELECTROMAGNETIC THEORY AND APPLICATION

N. Ida

Microwave NDT



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